- `www.cs.vu.nl/~gusz/ecbook/ecbook.html`
- `www.cems.uwe.ac.uk/~jsmith/ecbook/ecbook.html`

4. On this Web site we outline a full academic course based on this material.
5. There are slides to each chapter on the Web in PowerPoint and in PDF format. These slides can be freely downloaded and used to teach the material covered in the book.
6. All illustrations used on the slides are available separately from the Web as source (editable), PostScript, and JPG files. These enable readers to use and reuse them and to create their own versions for their own slides.
7. Furthermore, the Web site offers more exercises, answers to the exercises, downloadables for easy experimentation, errata, and a discussion group.

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We wish everybody a pleasant and fruitful time reading and using this book.

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Gusz Eiben and Jim Smith

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